Working with words frequencies

Natural Language Processing



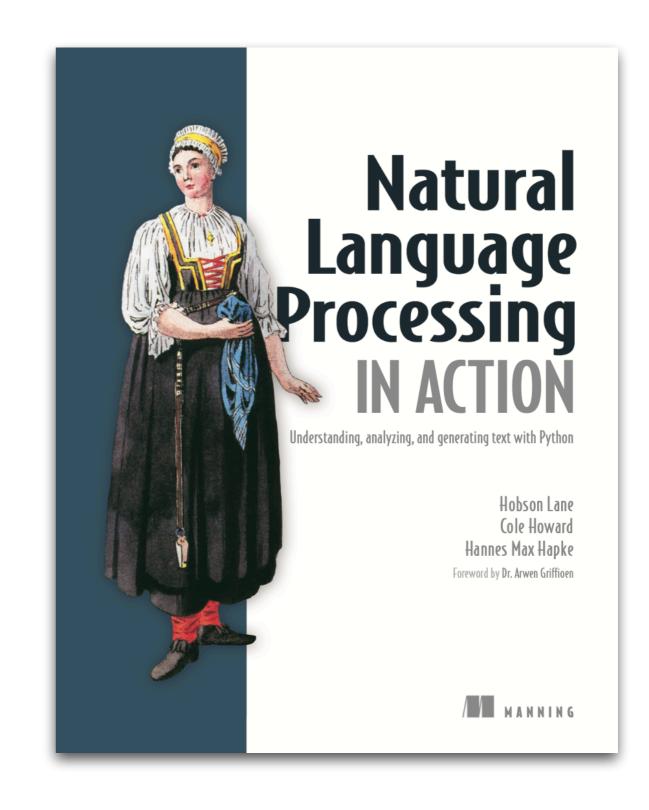
Lecture goals

- Counting term frequencies
- Represent document with vectors of term frequencies
- Finding relevant documents from a corpus using inverse document frequencies
- Estimating the similarity of pairs of documents with cosine similarity

Natural Language Processing in Action

by Hobson Lane Cole Howard Hannes Max Hapke

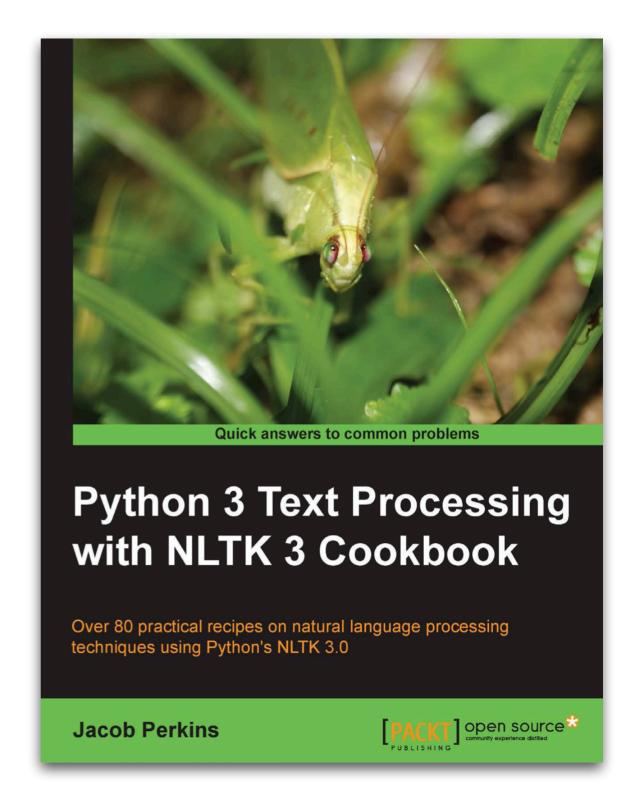
Manning Publications, 2019



Python 3 Text Processing with NLTK 3 Cookbook

by Jacob Perkins

Packt Publishing, 2014



Zipf's law

Zipf's law ([zif] or [tsipf] named after the American linguist George Kingsley Zipf although the French stenographer Jean-Baptiste Estoup appears to have noticed the regularity before Zipf) states that given some corpus of natural language utterances, the frequency of any word is inversely proportional to its rank in the frequency table. Thus the most frequent word will occur approximately twice as often as the second most frequent word, three times as often as the third most frequent word, etc.

If frequency is inversely proportional to rank, then the product of frequency and rank should be a constant:

$$r \cdot f = c$$

where *r* is the rank of a word in a text or group of texts, *f* the frequency of its occurrence and *c* is a constant value.

As a lot of real life things, not only linguistic, are governed by this law, so it usually refers to the "size" *y* of an occurrence of an *event* relative to it's rank *r*. Zipf's law states that **the "size" of the** *r***'th largest occurrence of the event is inversely proportional to it's rank**:

$$y \sim r^{-b}$$

where b is close to 1.0.

Zipf's law

CODE: Test Zipf's law

• lecture_03_01.py

Word counting

BOG (Bag Of Words) - quick remainder from last lecture

```
# -*- coding: utf-8 -*-
import pandas as pd
sentences = ["a b c d", "c d e f", "a b e f"]
tokens of sentences = [sentence.split() for sentence in sentences]
print(tokens of sentences)
bow = \{\}
for tokens in tokens of sentences:
    for token in tokens:
        bow[token] = 1
bow sorted = sorted(bow.items())
print(bow sorted)
corpus = {}
for index, tokens in enumerate(tokens of sentences):
    corpus['sentence {}'.format(index)] = dict(
        (token, 1) for token in tokens
df = pd.DataFrame.from records(corpus).fillna(0).astype(int).T
print(df)
```

```
[['a', 'b', 'c', 'd'],
['c', 'd', 'e', 'f'],
['a', 'b', 'e', 'f']]

[('a', 1), ('b', 1), ('c', 1),
('d', 1), ('e', 1), ('f', 1)]

a b c d e f
sentence_0 1 1 1 1 0 0
sentence_1 0 0 1 1 1 1
sentence_2 1 1 0 0 1 1
```

Word counting

Counter -> term frequency (TF)

The number of times a word occurs in a given document is called the *term frequency*, commonly abbreviated TF.

In some examples the count of word occurrences is normalized (divided) by the number of terms in the document.

Saying the truth, normalized frequency should rather be called a *probability*, but we will use term TF which is a common practice.

Anyway, regardless of the terminology, with both (simple counter or normalized counter) we can infer importance.

Term frequency (TF)

Simple case - single document

CODE

• lecture_03_02_01.py

Term frequency (TF)

Multiple documents

CODE

• lecture_03_02_02.py

Inverse document frequency (IDF)

Word counts for sure are useful, but pure word count, even when normalized by the length of the document, doesn't tell us much about the **importance of that word in that document** *relative* **to the rest of the documents** in the corpus.

For example, if we have a corpus of many books focused on the same topic or discipline, some words may occur many times in every document - that doesn't provide any new information as it doesn't help distinguish between those documents. On the other hand for sure there will be some words which are not so common across the entire corpus - they may exists in just a few of them and this is how we may know more about each document's nature.

So we need another tool, different than TF. Term frequencies must be weighted by something to ensure the most important, most meaningful words are given the highest value.

Inverse document frequency (IDF)

Inverse document frequency is the way we look in topic analysis through Zipf's law to bring out the most important details.

A good way to think of a term's inverse document frequency is this:

If a *term* appears in one document a lot of times and occurs rarely in the rest of the corpus, one could assume it's important to that document specifically. It could mean that this document is about this *term*.

Other words: if a *term* is rare among documents, but concentrate in one or few of them, it may be important. So, *term* importance is inversely proportional to its presence in all documents.

This way of thinking lead us to new definition. We define *inverse document frequency*, IDF in short, as the ratio of the total number of documents to the number of documents the term appears in.

This is how we can start very basic topic analysis.

Rule for TF:

The more times a word appears in the document, the TF (and hence the TF-IDF) will go up.

Rule for IDF:

As the **number of documents that contain a word goes up**, the IDF (and hence the TF-IDF) for that word will **go down**.

For a given term t, in a given document d, in a corpus (collection of documents) D we calculate TF-IDF as

$$tf(t,d) = \frac{count(t,d)}{count(d)} = \frac{\text{num of term } t \text{ in doc } d}{\text{num of all terms in doc } d}$$
$$idf(t,D) = \frac{count(D)}{count(t,D)} = \frac{\text{num of all docs in } D}{\text{num of docs from } D \text{ containing term } t}$$

$$tfidf(t, d, D) = tf(t, d) \cdot idf(t, D)$$

Why we need log()

Let's say, you have a huge collection of documents; for example 1000000 (1 million).

Now imagine that term *T1* is present in only 1 document, while *T2* in 10. Both 1 and 10 is a tiny drop compared to 1 million. When we count IDF for both terms we get

$$IDF_{T1} = \frac{1000000}{1} = 1000000$$

$$IDF_{T2} = \frac{1000000}{10} = 100000$$

That's a big difference in terms of Zipf's law. According to this law, when you compare the frequencies of two terms, like IDF's you have just calculated for *T1* and *T2*, even if they occur a similar number of times (which is in our case: 1 and 10 is quite similar, or close to each other, compared to 1 milion), the more frequent word (ranked higher) will have an *exponentially* higher frequency than the less frequent one

1 is 0.0001% of 1 million, 1000000 is 100% of 1 million

10 is 0.001% of 1 million, 100000 is 10% of 1 million

We may say that drawing all four percentage values on a number line, for fixed unit, 0.0001 is much closer to 0.001 than 10 to 100.

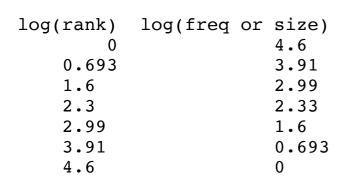
Why we need log()

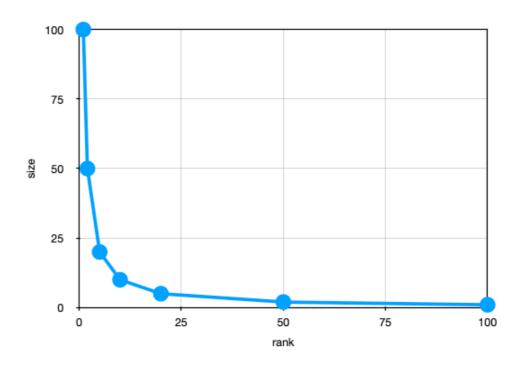
Do you remember? The frequency of any word is inversely proportional to its rank in the frequency table. The most frequent word will occur approximately twice as often as the second most frequent word, three times as often as the third most frequent word, etc.

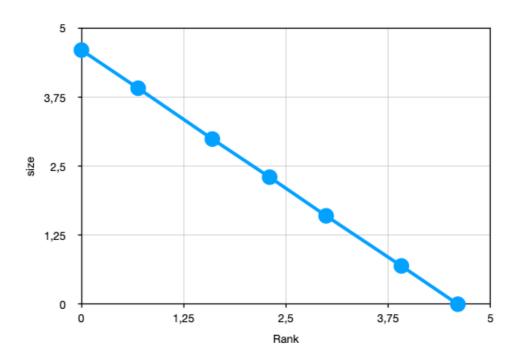
rank	freq or	r size	log(rank)	log(freq or	size)
1	100		0		4.6
2	50		0.693		3.91
5	20		1.6		2.99
10	10		2.3		2.33
20	5		2.99		1.6
50	2		3.91		0.693
100	1		4.6		0

Why we need log()

freq	or	size
100		
50		
20		
10		
5		
2		
1		
	100 50 20 10 5	50 20 10 5







Why we need log()

So Zipf's Law suggests that you scale all your frequencies (both for words and document) with the *log()* function which is the inverse of *exp()*. This ensures that terms such as *T1* and *T2* which have similar counts, aren't exponentially different in frequency. And this (log-log) distribution of word frequencies will ensure that your TF-IDF scores are more uniformly distributed.

For this reason, TF-IDF is calculated as

$$tf(t,d) = \frac{count(t,d)}{count(d)} = \frac{\text{num of term } t \text{ in doc } d}{\text{num of all terms in doc } d}$$

$$idf(t,D) = log\left(\frac{count(D)}{count(t,D)}\right) = log\left(\frac{\text{num of all docs in }D}{\text{num of docs from }D\text{ containing term }t}\right)$$

$$tfidf(t, d, D) = tf(t, d) \cdot idf(t, D)$$

Some notes

TF-IDF relates a specific word or token *t* to a specific document *d* in a specific corpus *D*, and then **it assigns a numeric value to the** *importance* **of that word in the given document, given its usage across the entire corpus**.

Sometimes we make all the calculations in log space:

 $tfidf(t, d, D) = log(tf(t, d)) \cdot log(idf(t, D))$

Create K-dimensional vector representation of each document in the corpus.

CODE

• lecture_03_03.py

How to measure similarity

- With euclidean distance
- With cosine similarity

Cosine similarity

$$\cos\Theta = \frac{A \cdot B}{|A| |B|}$$

A cosine similarity of 1 represents vectors that point in exactly the same direction; the vectors may have different lengths or magnitudes.

When a cosine similarity is close to 1, we know that the documents are using similar words in similar proportion. So the documents whose document vectors are close to each other are likely talking about the same thing.

Documents relevance

In the last lecture you used BOW (bag-of-words) vectors to find documents overlap.

Extension of BOW with simple words counting (and even words frequency - TF) isn't a big step forward.

You get a new value replacing each word's counter (TF) with the word's TF-IDF. With this your vectors will more thoroughly reflect the meaning, or topic, of the document

Documents relevance

Compute a new document relevance in context of corpus we have.

CODE

• lecture 03 04.py

Speedup with indexing

Forward and inverse index

In computer science, an *inverted index* is a database index storing a mapping from content, such as words or numbers, to its locations in a table, or in a document or a set of documents. It is named *inverted* in contrast to a *forward index*, which maps from documents to content.

There is no real technical distinction between a forward index and an inverted index. An inverted index is just an index... but backwards. The concept of an inverted index only makes sense if the concept of a regular (forward) index already exists. Other words, first you need to have something to be able to talk about inverting (it).

"Forward" and "inverted", in the context of a search engine, are just descriptive terms to distinguish between:

- A list of words contained in a document.
- A list of documents containing a word.

For example, forward index would store

```
{ Document1: ["Text", "from", "a", "document", "number", "1"],
...
},
an inverted index would store:
{ "Text": [Document1, Document100, ...],
    "from": [Document1, Document2, ...],
...
```

One lets you look up a document and find the contents, the other lets you look up a word and get a list of documents.

Speedup with indexing

Forward and inverse index

Advantage of inverted index is:

 Inverted index is to allow fast full text searches, at a cost of increased processing when a document is added to the database.

Disadvantage of inverted index is:

 Large storage overhead and high maintenance costs on update, delete and insert.

You can say this:

- Forward index: fast indexing, less efficient query's
- Inverted index: fast query, slower indexing

Another kind of speedup

What about vectors with only relevant words?

How we can use it in chatbot

But most chatbots rely heavily on a search engine. And some chatbots rely exclusively on a search engine as their only algorithm for generating responses. You need to take one additional step to turn your simple search index (TF-IDF) into a chatbot. You need to store your training data in pairs of questions (or statements) and appropriate responses. Then you can use TF-IDF to search for a question (or statement) most like the user input text. Instead of returning the most similar statement in your database, you return the response associated with that statement.

Bibliography

- [Lan] Hobson Lane, Cole Howard, Hannes Max Hapke, Natural Language Processing in Action, Manning Publications, 2019
- [Per] Jacob Perkins, Python 3 Text Processing with NLTK 3 Cookbook, Packt Publishing, 2014